



**APPLICATIONS OF THE BERRN-ESSEN INEQUALITY  
TO LIMIT THEOREMS FOR RANDOM ADDITIONS**

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Uniformly distributed, indiscriminate

$$\xi_1, \xi_2, \dots, \xi_n, \dots \tag{1}$$

given a sequence of random quantities, i.e.

$$F(x) = P\{\xi < x\}, \quad M\xi = a, \quad D\xi = \sigma^2, \quad \beta_3 = M|\xi - a|^3.$$

The following  $v = v(1)$  random quantity  $\lambda > 0$  depends on the parameter and (1) does not depend on random quantities and

$$Mv(\lambda) = \sum_{k=1}^{\infty} kp_k = \alpha,$$

$$Dv(\lambda) = \sum_{k=1}^{\infty} (k - \alpha)^2 p_k = \gamma^2.$$

(1) from  $v = v(\lambda)$  depending on

$$(2) \eta_v = \sum_{i=1}^v \xi_i \tag{2}$$

we make the sum.

Its distribution function is

$$F_{v(\lambda)}(x) = P(\eta_v < x)$$

S.G. The inequality given by S.G.Essen is

$$|F_n(x) - \Phi(x)| < c \frac{\beta_3}{\sqrt{n}},$$

in terms of visibility, this inequality is given by Y.V.Prokhorov in terms of this flat estimate

$$|F_n(x) - \Phi(x)| < c \frac{\beta_3}{\sqrt{n}} - \frac{1}{1 + |x|^3},$$

and generalized from the Berry side.

$$\Phi(x) = \frac{1}{\sigma\sqrt{2\pi}} \int_{-\infty}^x e^{-\frac{(t-a)^2}{2\sigma^2}} dt$$

This article explores the generalization of theorems by applying the Berry-Essen inequality of non-planar estimates given for assigned random quantities. Theorem. If  $\beta_3 < \infty$  and  $\beta_3 < \infty$ , then

$$|F_{v(\lambda)}(x) - \Phi(x)| \leq c_1 \left[ \frac{\beta_3}{\sqrt{\alpha}} \cdot \frac{1}{\sigma^3(1+x^2)} + \frac{\gamma}{\alpha} \right] \quad (3)$$

The isiubot of the theorem is proved by applying a complete probability formula, using P.L.Chebichev's inequality.

If  $P(v(\lambda) - k) = P_k$  is said, then the Berry-Essen inequality from (3) follows and generalizes.

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